

# Model-based (sensorless) collision detection and localization

DEPARTMENT OF COMPUTER, CONTROL, AND  
MANAGEMENT ENGINEERING ANTONIO RUBERTI

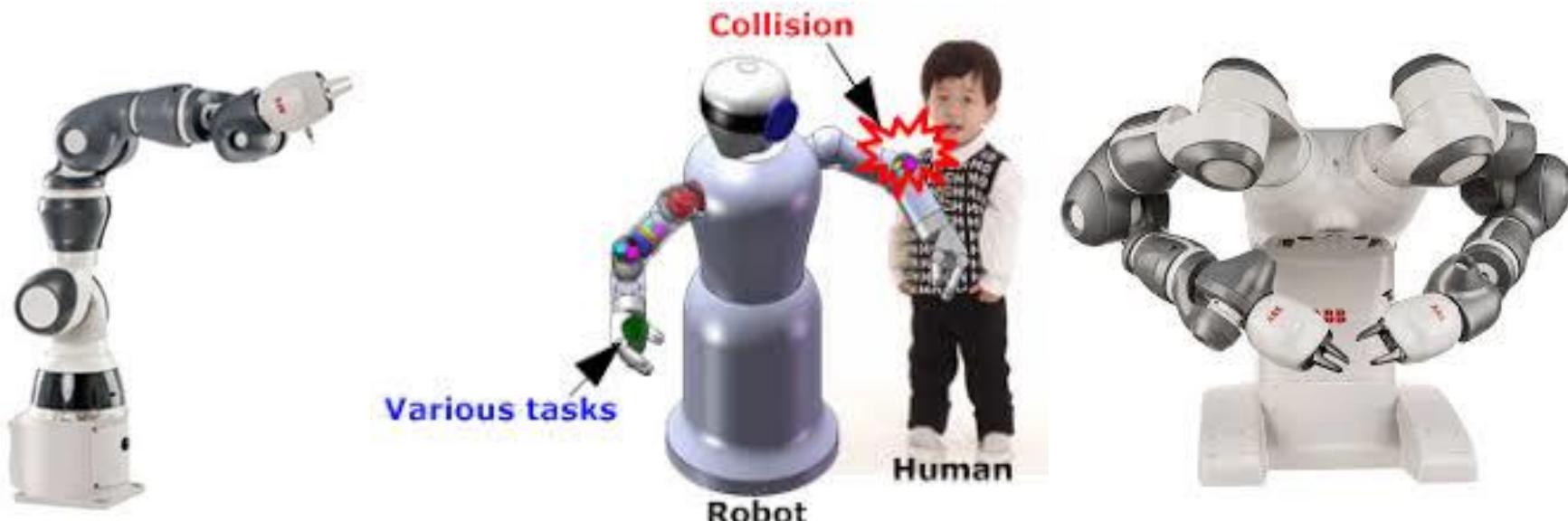


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# Introduction

- Collision monitoring for safe pHRI with residual method based on generalized momentum
- Simulations on YuMi (ABB, 2015): lightweight collaborative robot with two 7R arms



# The residual method for collision detection and localization

## Residual dynamics - 1

$$\mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f = \boldsymbol{\tau}_m + \boldsymbol{\tau}_k$$

$$\dot{\mathbf{r}} = \mathbf{K}_o(\boldsymbol{\tau}_k - \mathbf{r})$$

$$\mathbf{r}(0) = \mathbf{r}_0 = \mathbf{0}$$

- AS, linear and decoupled residual dynamics
- No initial transient, only excited by collisions
- No additional sensors (sensorless)
- No inertia matrix inversion
- No joint acceleration estimation

## Residual dynamics - 2

$$\dot{\mathbf{r}} = \mathbf{K}_o(\boldsymbol{\tau}_k - \mathbf{r})$$

$\boldsymbol{\tau}_k$  not available for implementation: using robot model

$$\mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f = \boldsymbol{\tau}_m + \boldsymbol{\tau}_k$$

it is obtained

$$\dot{\mathbf{r}} = \mathbf{K}_o(\mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f - \boldsymbol{\tau}_m - \mathbf{r})$$

## Residual dynamics - 3

$$\dot{\mathbf{r}} = \mathbf{K}_o(\mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f - \boldsymbol{\tau}_m - \mathbf{r})$$

Joint acceleration estimation required:  
introducing robot generalized momentum

$$\mathbf{p} = \mathbf{M}(\mathbf{q})\dot{\mathbf{q}}$$

$$\dot{\mathbf{p}} = \mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \dot{\mathbf{M}}(\mathbf{q})\dot{\mathbf{q}}$$

it is obtained

$$\dot{\mathbf{r}} = \mathbf{K}_o(\dot{\mathbf{p}} - \dot{\mathbf{M}}(\mathbf{q})\dot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f - \boldsymbol{\tau}_m - \mathbf{r})$$

## Residual dynamics - 4

$$\dot{\mathbf{r}} = \mathbf{K}_o(\dot{\mathbf{p}} - \dot{\mathbf{M}}(\mathbf{q})\dot{\mathbf{q}} + \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f - \boldsymbol{\tau}_m - \mathbf{r})$$

Defining for compactness

$$\beta(\mathbf{q}, \dot{\mathbf{q}}) := \mathbf{c}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) + \boldsymbol{\tau}_f - \dot{\mathbf{M}}(\mathbf{q})\dot{\mathbf{q}}$$

$$\hat{\mathbf{p}} := \mathbf{r} - \beta(\mathbf{q}, \dot{\mathbf{q}}) + \boldsymbol{\tau}_m$$

it is obtained

$$\dot{\mathbf{r}} = \mathbf{K}_o(\dot{\mathbf{p}} - \hat{\mathbf{p}})$$

## Residual dynamics - 5

$$\dot{\mathbf{r}} = \mathbf{K}_o(\dot{\mathbf{p}} - \hat{\dot{\mathbf{p}}})$$

$\dot{\mathbf{p}}$  not available for implementation: applying integral operator

$$\hat{\mathbf{p}} = \int_0^t (\mathbf{r} - \boldsymbol{\beta}(\mathbf{q}, \dot{\mathbf{q}}) + \boldsymbol{\tau}_m) dt$$

it is obtained

$$\mathbf{r} = \mathbf{K}_o(\mathbf{p} - \mathbf{p}_0 - \hat{\mathbf{p}})$$

# Collision detection

$$\dot{\mathbf{r}} = \mathbf{K}_o(\boldsymbol{\tau}_k - \mathbf{r})$$

- Residuals: excited iff a collision happens
- Monitoring signal: norm of the residual vector
- Threshold to balance false negatives and false positives

## Contact link isolation

Jacobian on link i: no dependence on joints i+1 to n

$$\mathbf{J}_c(\mathbf{q}) = [* * * | \mathbf{O}]$$

Collision on link i: no effect on residuals i+1 to n

$$\boldsymbol{\tau}_k = \mathbf{J}_c^T(\mathbf{q}) \mathcal{F}_{ext}$$

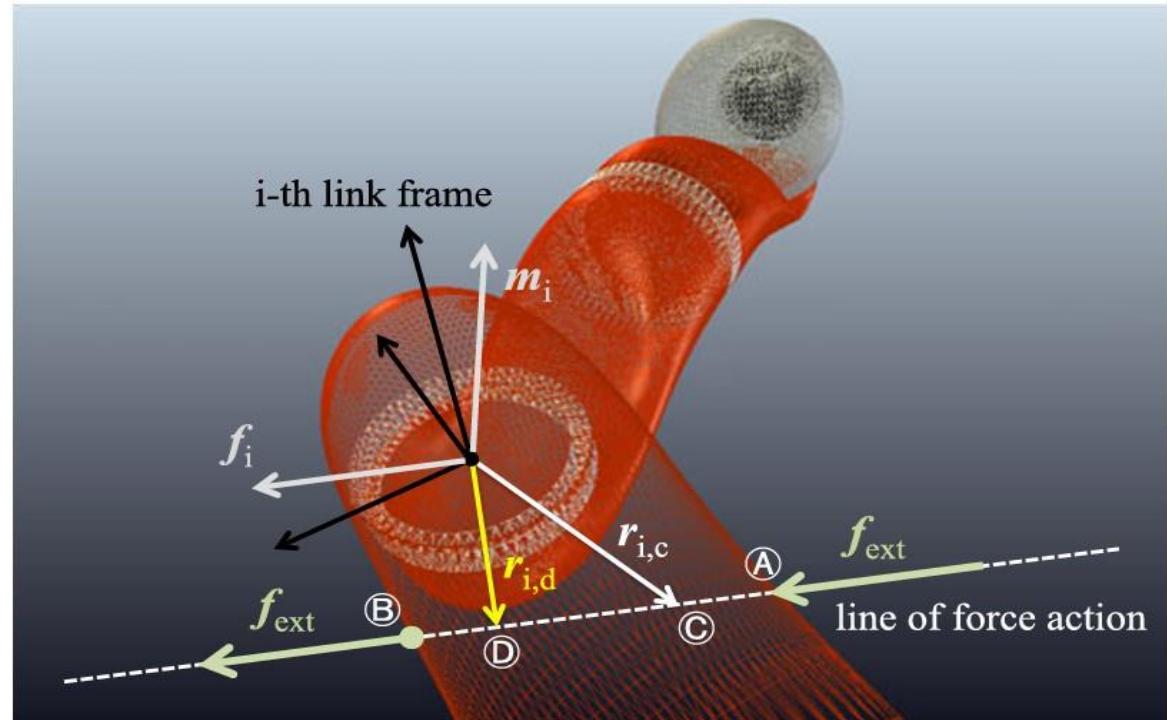
$$i_c = \max\{i \in \{1, \dots, n\} : r_i \neq 0\}$$

# Contact point isolation

Transformation between contact point and origin of frame i

$$\mathcal{F}_i = \mathbf{J}_{c,i}^T \mathcal{F}_{ext}$$

$$\mathbf{J}_c(\mathbf{q}) = \mathbf{J}_{c,i} \mathbf{J}_i(\mathbf{q})$$



$$\mathbf{J}_{c,i} = \begin{bmatrix} \mathbf{I}_{3 \times 3} & -\mathbf{S}({}^0\mathbf{r}_{i,c}) \\ \mathbf{O}_{3 \times 3} & \mathbf{I}_{3 \times 3} \end{bmatrix}$$

# Contact point isolation

$\hat{\mathbf{r}}$  estimator for  $\tau_k$  for  $K_o$  big enough

$$\hat{\mathcal{F}}_i = (\mathbf{J}_i^T(\mathbf{q}))^\# \mathbf{r}$$

$$\mathcal{F}_{ext} = \begin{bmatrix} \mathbf{f}_{ext} \\ \mathbf{0}_{3 \times 1} \end{bmatrix}$$

From the force transformation:

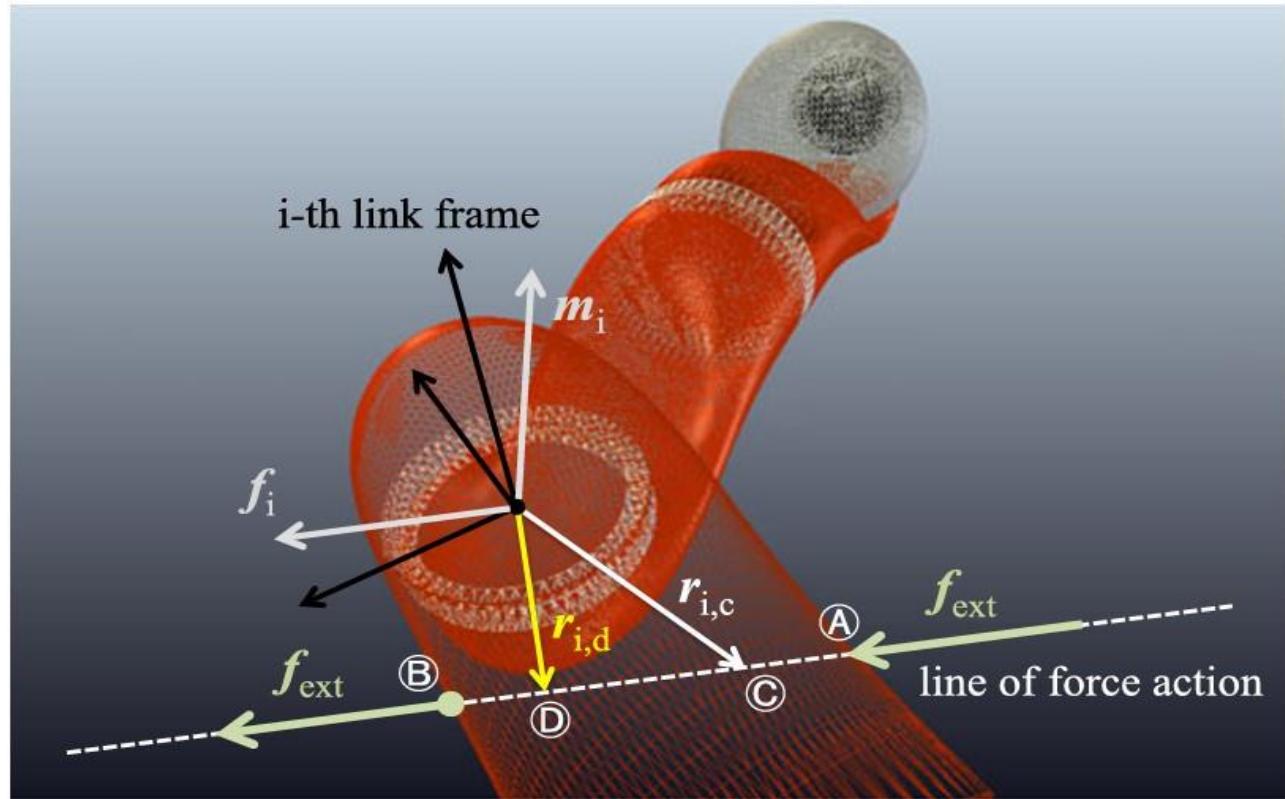
$$\hat{\mathcal{F}}_i = \begin{bmatrix} \hat{\mathbf{f}}_i \\ \hat{\mathbf{m}}_i \end{bmatrix} = \begin{bmatrix} \mathbf{I}_{3 \times 3} & \mathbf{O}_{3 \times 3} \\ -\mathbf{S}^T(\mathbf{r}_{i,c}) & \mathbf{I}_{3 \times 3} \end{bmatrix} \begin{bmatrix} \mathbf{f}_{ext} \\ \mathbf{0}_{3 \times 1} \end{bmatrix}$$

$$\hat{\mathbf{m}}_i = \mathbf{S}^T(\hat{\mathbf{f}}_i) \mathbf{r}_{i,c}$$

# Contact point isolation

$$\hat{\mathbf{m}}_i = \mathbf{S}^T(\hat{\mathbf{f}}_i)^0 \mathbf{r}_{i,c}$$

Rank = 2  
Solution: subspace of dimension 1



$${}^0\mathbf{r}_{i,d} = (\mathbf{S}^T(\hat{\mathbf{f}}_i))^{\#} \hat{\mathbf{m}}_i$$

$${}^0\mathbf{r}_{i,c} = {}^0\mathbf{r}_{i,d} + \lambda \frac{\hat{\mathbf{f}}_i}{\|\hat{\mathbf{f}}_i\|}$$

# Contact wrench identification

Contact point Jacobian is now known

$$\boldsymbol{\tau}_k = \mathbf{J}_c^T(\mathbf{q}) \mathcal{F}_{ext}$$

$\mathbf{r}$  estimator for  $\boldsymbol{\tau}_k$  for  $\mathbf{K}_o$  big enough

$$\hat{\mathcal{F}}_{ext} = (\mathbf{J}_c^T(\mathbf{q}))^\# \mathbf{r}$$

# Limits of the residual method

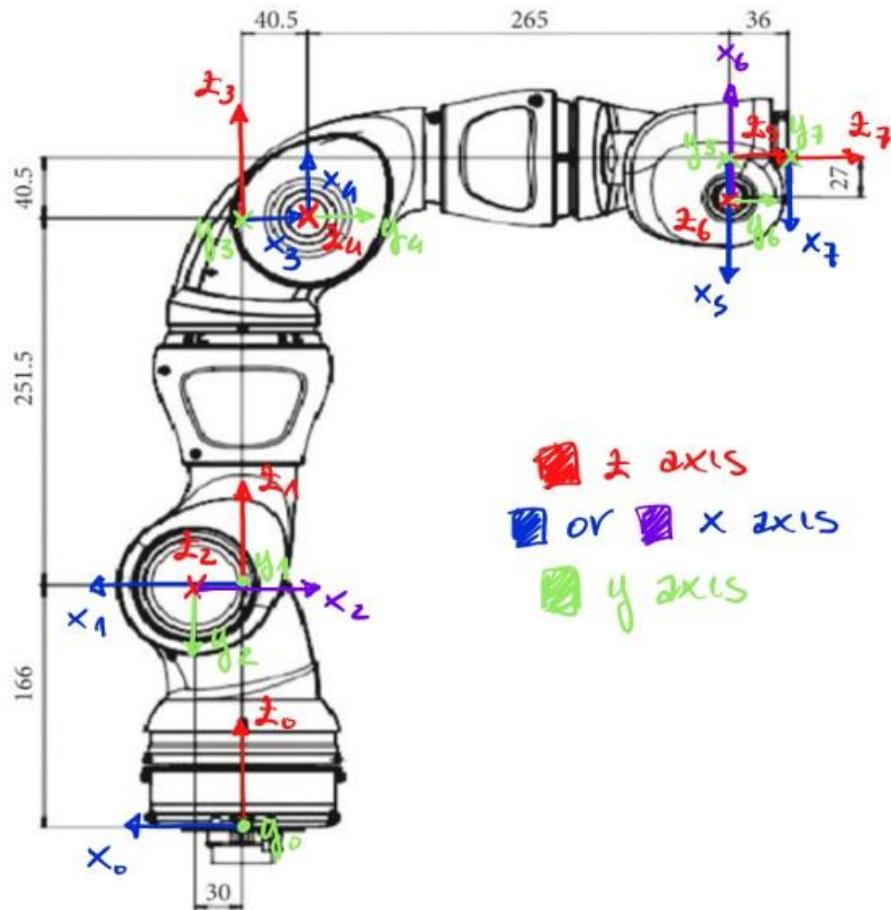
- Compromise for  $K_o$ 
  - small  $K_o$  to limit initial transient
  - big  $K_o$  to have  $\tau_k$  estimated by  $r$
- Collision detectable iff produce work
- Jacobian not full rank for  $i < 6$  or in singularities
- Requires model knowledge (model-based)

# Kinematic and dynamic model of the ABB YuMi robot

# Model

- The dynamic model is generated using the software openSYMORO, using Newton-Euler algorithm
- openSYMORO requires the use of the modified DH convention
- Generated code leads to faster simulations than our custom NE implementation

# Kinematic model



$i$	$\alpha_i$ [rad]	$a_i$ [m]	$d_i$ [m]	$\theta_i$ [rad]
1	0	0	0.166	$q_1$
2	$\pi/2$	0.03	0	$q_2$
3	$\pi/2$	0.03	0.2515	$q_3$
4	$-\pi/2$	0.0405	0	$q_4$
5	$-\pi/2$	0.0405	0.265	$q_5$
6	$-\pi/2$	0.027	0	$q_6$
7	$-\pi/2$	0.027	0.036	$q_7$

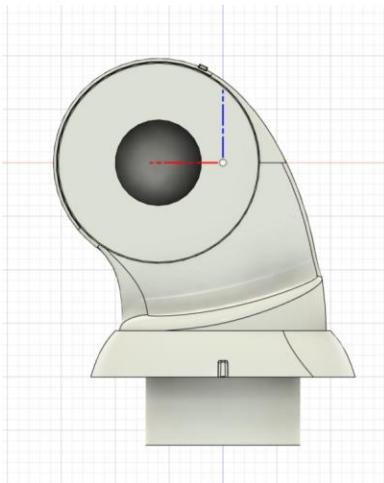
DHM table

$$\mathbf{q} = \begin{bmatrix} 0 & \pi & 0 & -\frac{\pi}{2} & \pi & \pi & \pi \end{bmatrix}^T$$

# Dynamic model

- Inertial parameters are obtained via CAD analysis in Autodesk Fusion 360
- 3D .step files are provided by ABB for each link
- In CAD links are matched to their DHM configuration
- Material is set to magnesium AZ63A, to match material (generic "magnesium alloy") and weight (9.5kg) mentioned in the product page

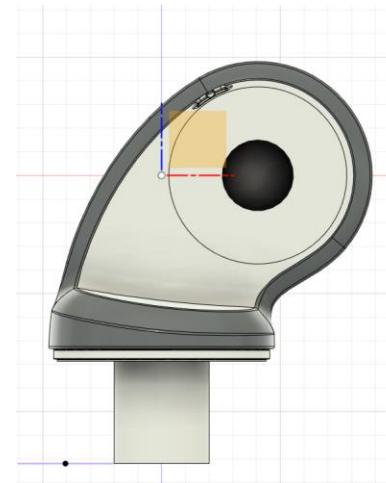
# Links in CAD



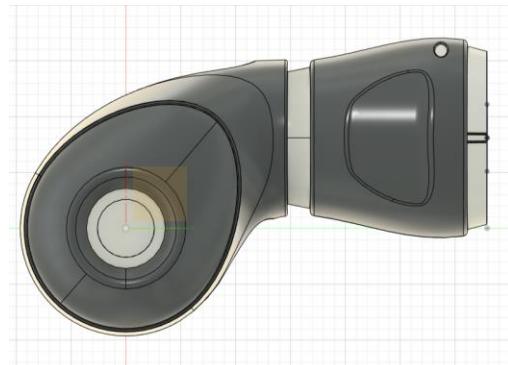
Link 1



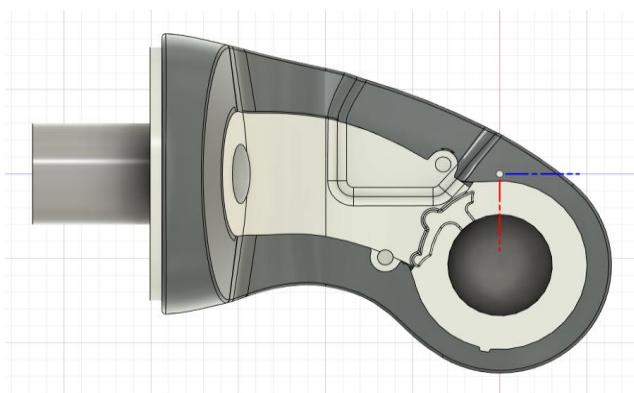
Link 2



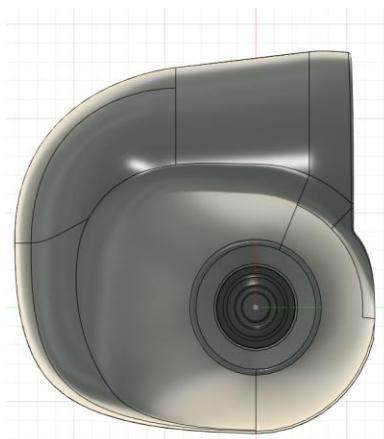
Link 3



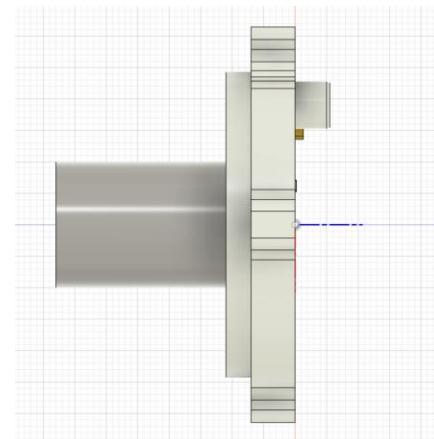
Link 4



Link 5



Link 6



Link 7

# Dynamic model

Parameter	Link 1	Link 2	Link 3	Link 4	Link 5	Link 6	Link 7
$m$ [kg]	1.761	2.577	1.408	2.158	0.628	0.859	0.056
$CoM_x$ [m]	0.009	0.017	0.019	0.023	0.007	0.011	0
$CoM_y$ [m]	-0.023	-0.063	0.026	0.056	0.027	-0.012	-0.001
$CoM_z$ [m]	-0.05	-0.013	-0.035	-0.017	-0.054	-0.01	-0.011
$XX$ [kg m <sup>2</sup> ]	0.011	0.024	0.007	0.017	0.004	0.001	$1.980 \cdot 10^{-5}$
$XY$ [kg m <sup>2</sup> ]	0.001	0.005	-0.001	-0.005	0	0	$\approx 0$
$XZ$ [kg m <sup>2</sup> ]	0	0	0	0	0	0	$\approx 0$
$YY$ [kg m <sup>2</sup> ]	0.01	0.005	0.007	0.005	0.003	0.001	$1.971 \cdot 10^{-5}$
$YZ$ [kg m <sup>2</sup> ]	0	0	0	0	0	0	$\approx 0$
$ZZ$ [kg m <sup>2</sup> ]	0.004	0.024	0.004	0.017	0.001	0.001	$1.578 \cdot 10^{-5}$

## Uncertain model

- Up to 20% uncertainty on dynamical parameters is considered
- Uncertainty is represented as a multiplicative constant on inertial parameters ranging from 0.8 to 1.2
- Three different constants for each link (21 in total), one each for
  - Elements of the inertia matrix
  - Center of mass
  - Mass

# Implementation

- Code generated by openSYMORO is converted into MATLAB code for simulation. Functions for:
  - Inertia matrix  $M(q)$
  - Nonlinear terms  $n(q, dq)$
  - Jacobian of frame  $i$   $J_i(q)$
  - Gravity terms are obtained by  $g(q) = n(q, 0)$
- Uncertainties are randomly generated with uniform distribution when simulation starts

# Simulations on the ABB YuMi robot

# General scheme

- Robot dynamics is simulated in continuous time with `ode45`
- Control and residual dynamics are computed in discrete time, 1ms sampling time
- Control uses a ZOH
- For residual:
  - Integral term approximated with Euler
  - Approximate derivative

$$\dot{M}_k(\mathbf{q}) \approx \frac{M_k(\mathbf{q}) - M_{k-1}(\mathbf{q})}{T_s}$$

# Controller

- Feedback Linearization controller

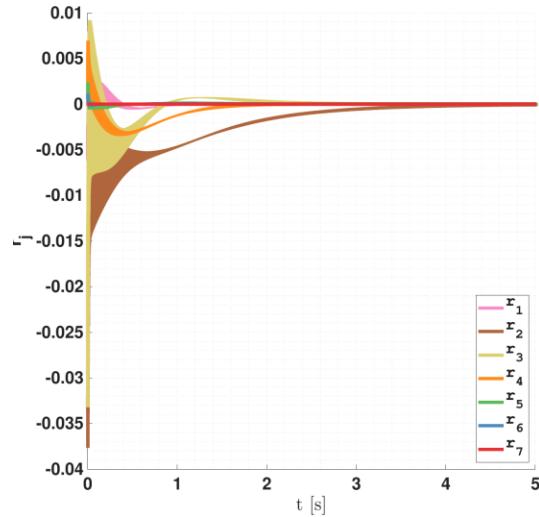
$$\tau_m = \hat{M}(q)(\ddot{q}_d + K_p(q_d - q) + K_d(\dot{q}_d - \dot{q})) + \hat{n}(q, \dot{q})$$

- For regulation task

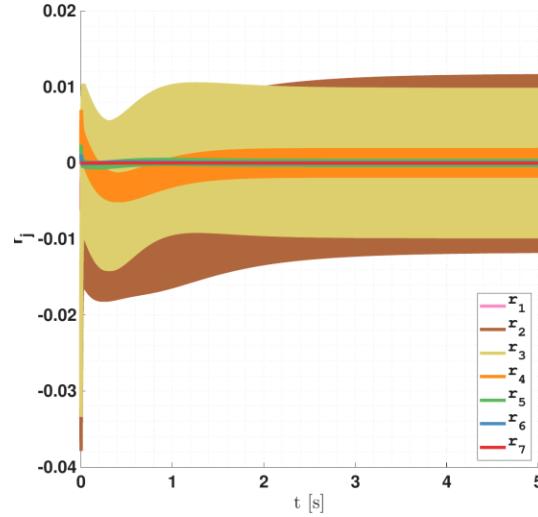
$$\tau_m = \hat{M}(q)(K_p(q_d - q) - K_d\dot{q}) + \hat{n}(q, \dot{q})$$

$$K_p = \text{diag}\{200\} \quad K_d = \text{diag}\{200\}.$$

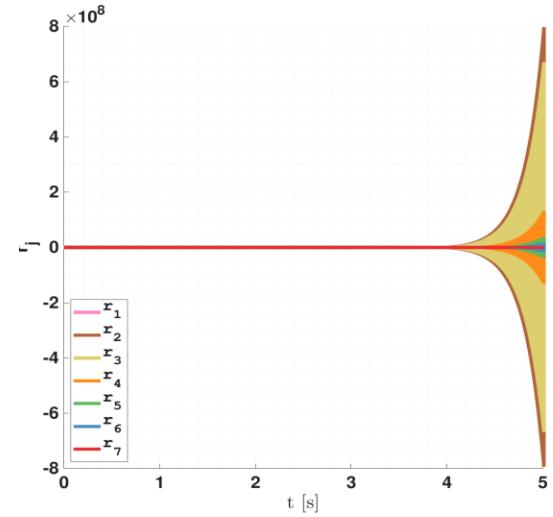
# Ko tuning and stability of residual dynamics



$$K_o = 1995 \text{ s}^{-1}$$



$$K_o = 2000 \text{ s}^{-1}$$

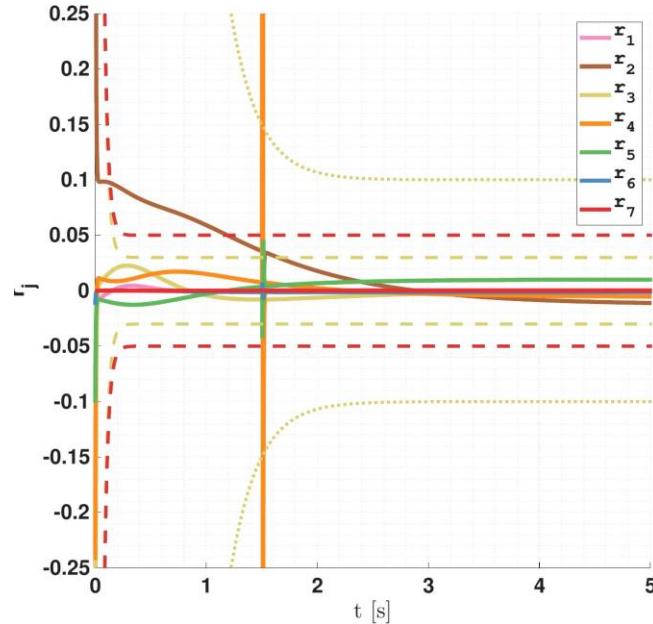


$$K_o = 2005 \text{ s}^{-1}$$

Final choice:  $K_o = 1000 \text{ s}^{-1}$

# Thresholds tuning

- Force modelling:  
 $10N \leq \|f\| \leq 500N$
- Threshold:negative exponential for transient + steady state constant value
- Tuning with a force  
 $\|f\| = 10N$

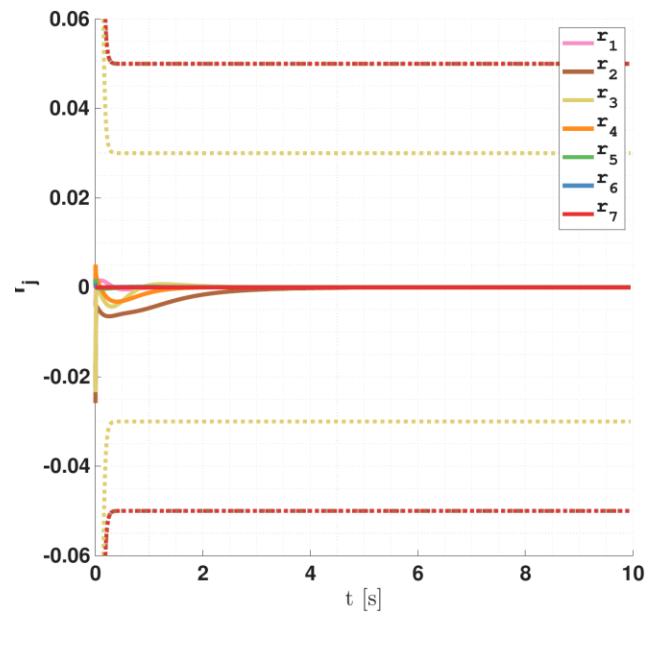
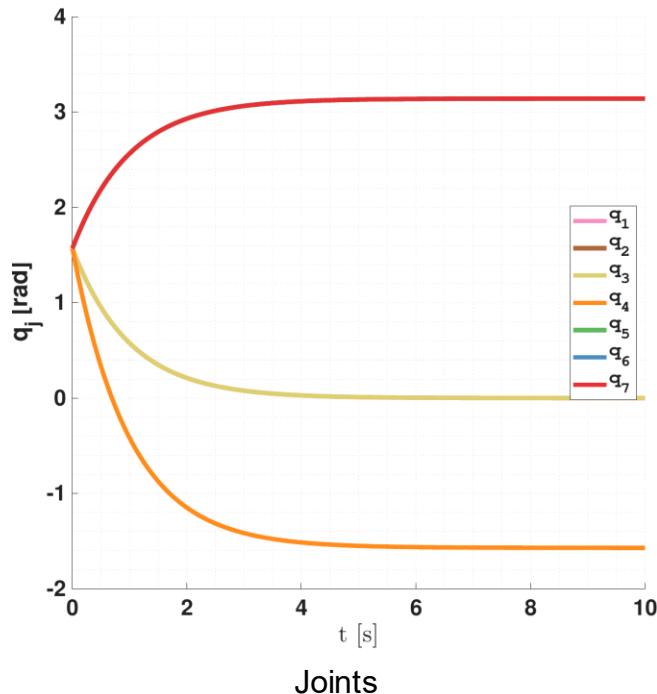


$$\epsilon_{nom} = [0.05 \ 0.05 \ 0.03 \ 0.05 \ 0.05 \ 0.05 \ 0.05]^T \cdot e^{1-30t}$$

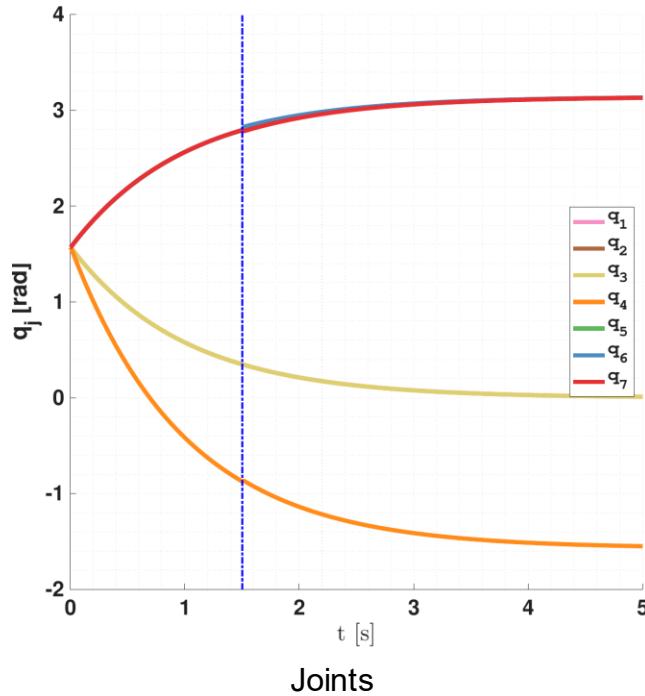
$$\epsilon_{unc} = [1 \ 1.2 \ 0.1 \ 1 \ 1 \ 1 \ 1]^T \cdot e^{3-4t}$$

# Task 1: regulation

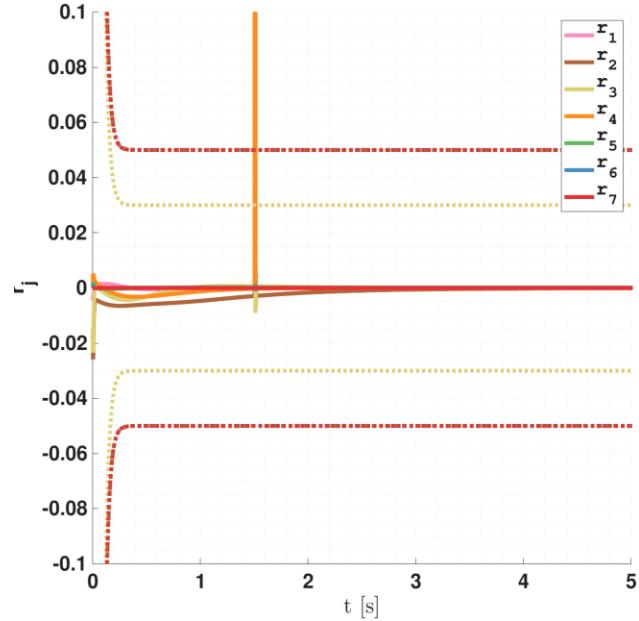
- Desired (rest) position:  $q_d = \begin{bmatrix} 0 & \pi & 0 & -\frac{\pi}{2} & \pi & \pi & \pi \end{bmatrix}^T$
- Initial (rest) position:  $q_0 = \begin{bmatrix} \frac{\pi}{2} & \frac{\pi}{2} & \frac{\pi}{2} & \frac{\pi}{2} & \frac{\pi}{2} & \frac{\pi}{2} & \frac{\pi}{2} \end{bmatrix}^T$



# Collision link 4 – 100 N (nominal case)



Joints



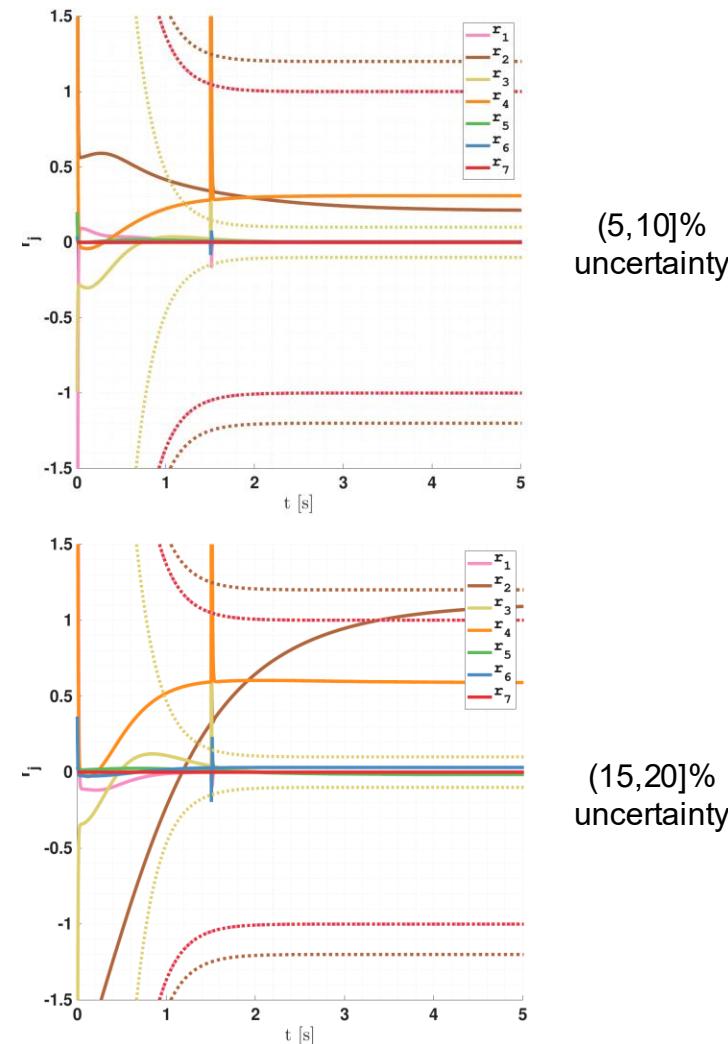
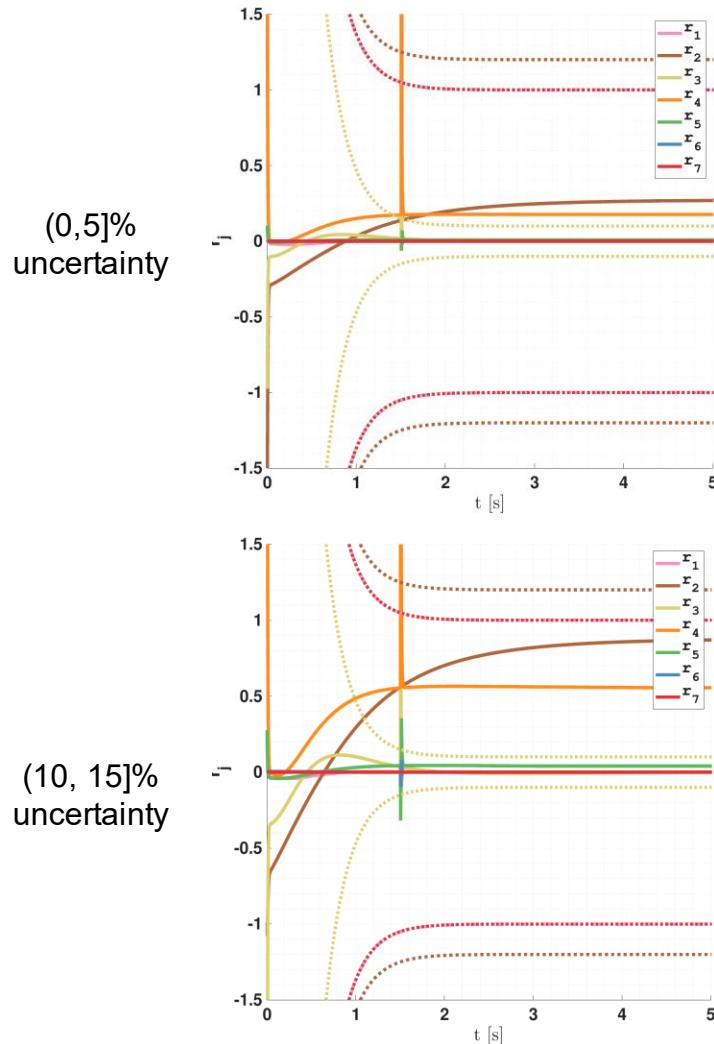
Residuals

$${}^0\mathbf{r}_{4,d} = \begin{bmatrix} -0.0017 \\ -0.0007 \\ 0.0142 \end{bmatrix} \text{ m}$$

$$\hat{\mathcal{F}}_{ext} = \begin{bmatrix} 59.3696 \\ 49.6715 \\ -4.8100 \\ 1.4515 \\ 1.2157 \\ -0.1168 \end{bmatrix} \begin{bmatrix} \text{N} \\ \text{Nm} \end{bmatrix}$$

- Collision correctly detected on link 4 at  $t=1.501$  s
- Isolation and identification not accurate (  $\rho(J) = 4$  )

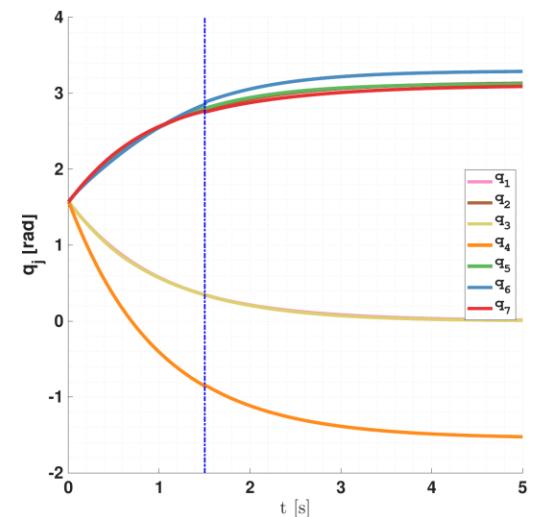
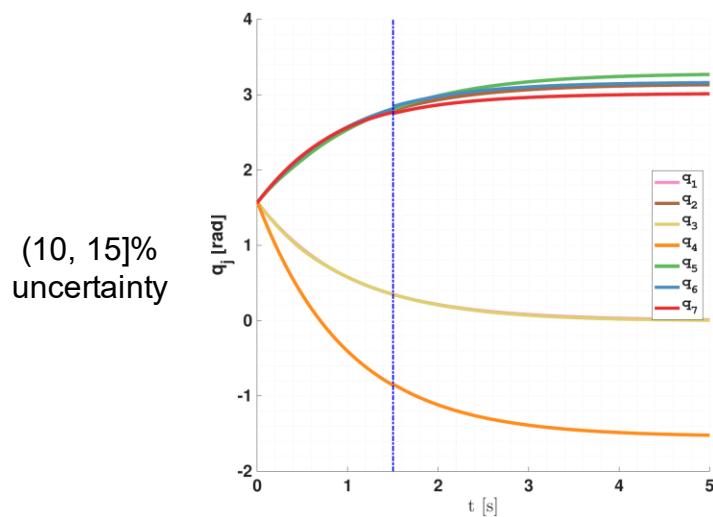
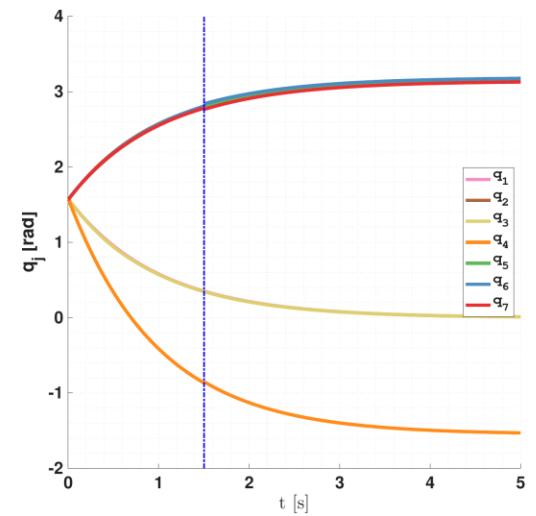
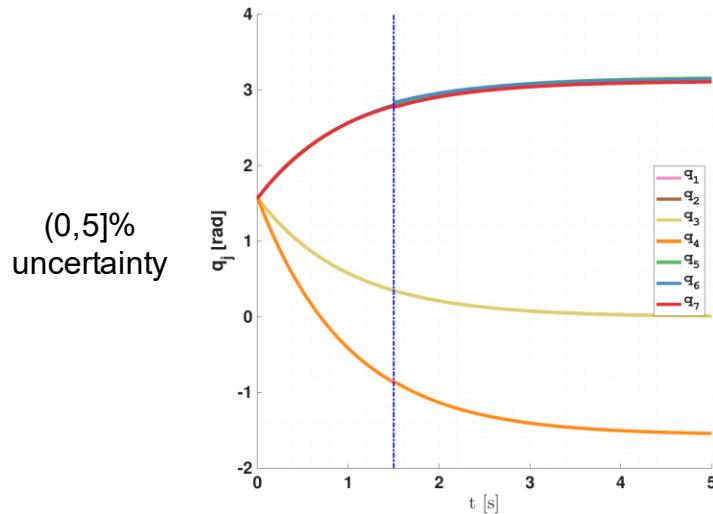
# Collision link 4 – 100 N (uncertain residuals)



(10, 15)%  
uncertainty

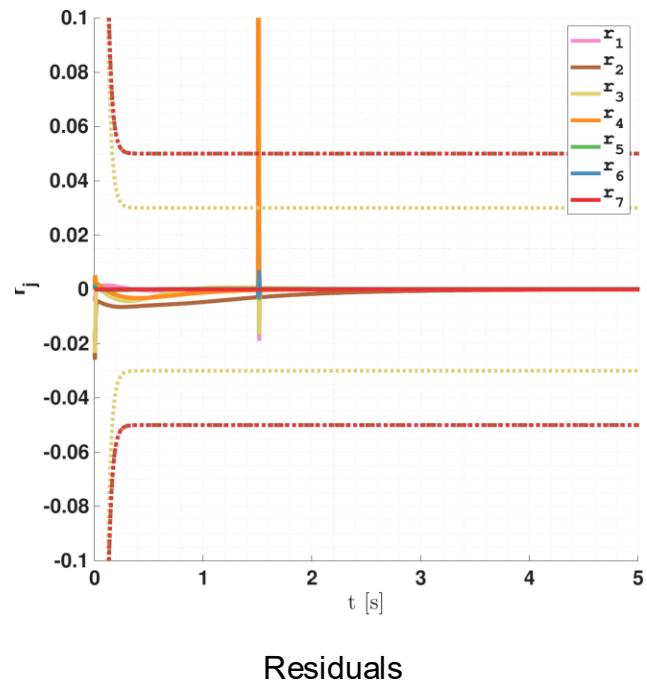
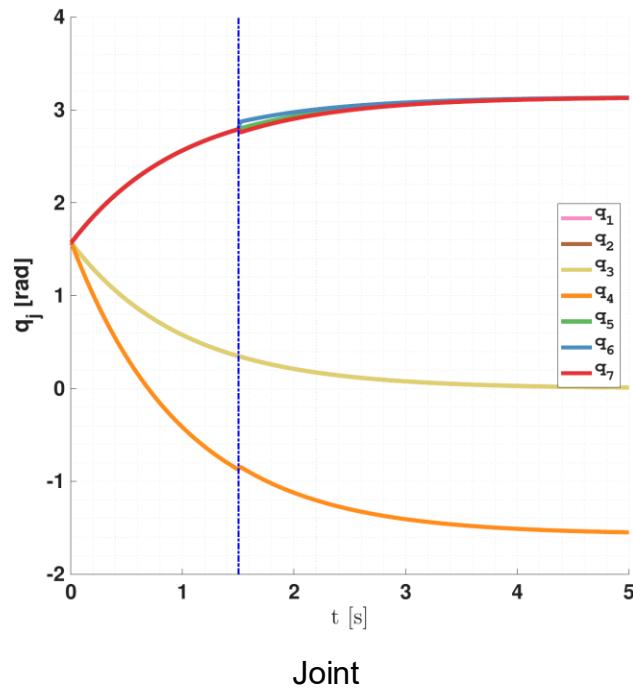
(15, 20)%  
uncertainty

# Collision link 4 – 100 N (uncertain joints)



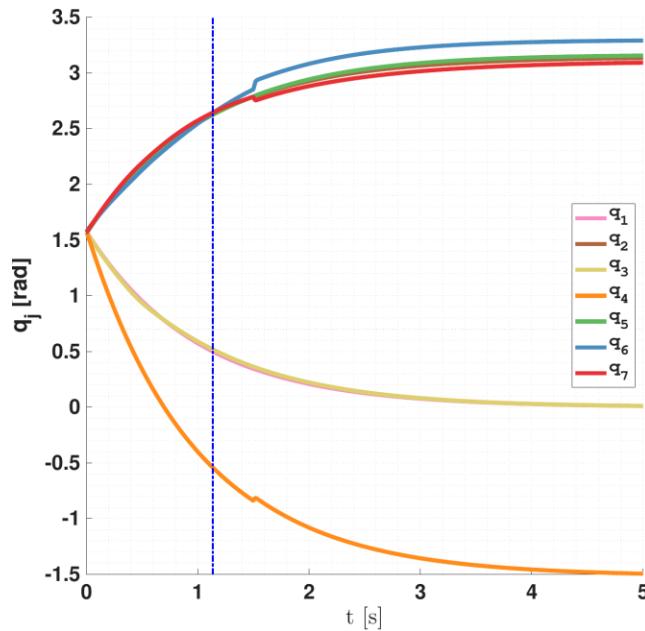
# Collision link 4 – 250 N (nominal case)

- Collision correctly detected at  $t=1.501s$

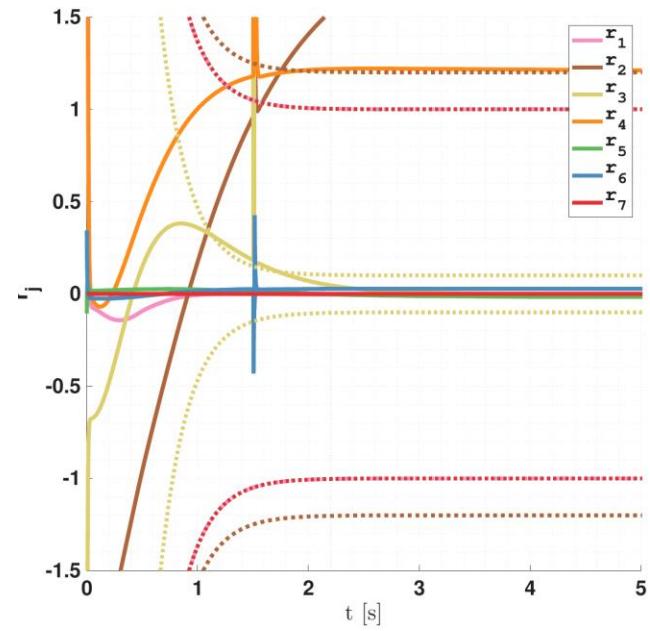


# Collision link 4 – 250 N

- Joints and residuals with (15,20)% uncertainty
- False positive on link 3 at t=1.137s



Joints



Residuals

## Collision link 6 – off origin

- Collision force chosen to avoid huge changes in joint configuration
- Collision point simulated on outer shell of the link
- Expected isolation result is the minimum distance between the line of action of the force and origin of frame 6

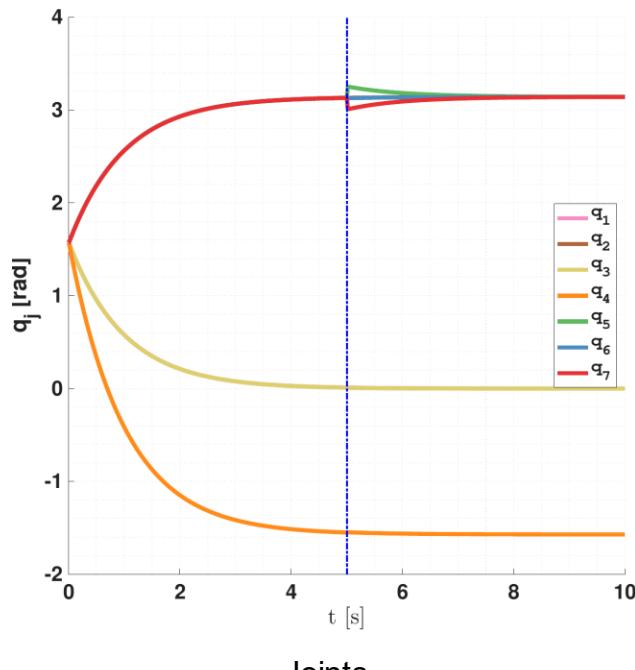
$$\mathcal{F}_{ext} = \begin{bmatrix} 0 \\ -10 \\ 0 \end{bmatrix} \text{ N}$$

$${}^0\mathbf{r}_{6,c} = \begin{bmatrix} 0.05 \\ 0.03 \\ 0 \end{bmatrix} \text{ m}$$

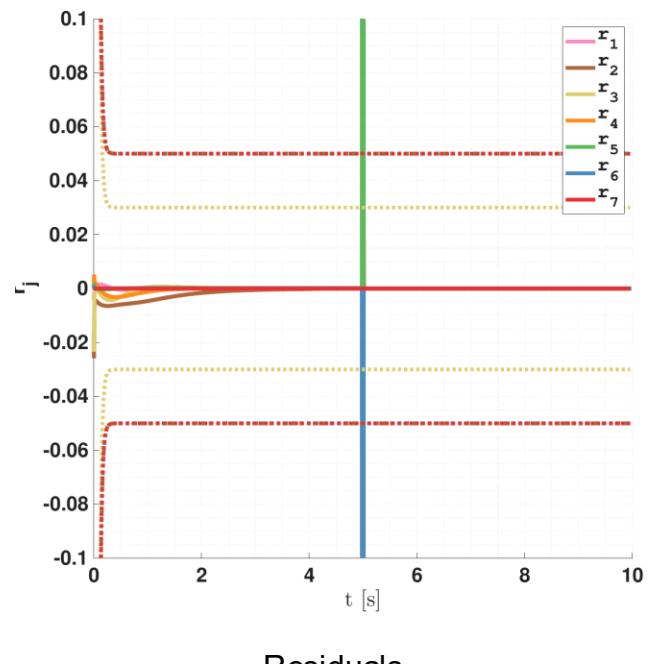
$${}^0\mathbf{r}_{6,d} = \begin{bmatrix} 0.05 \\ 0 \\ 0 \end{bmatrix} \text{ m}$$

# Collision link 6 – off origin

- Nominal joints and residuals



Joints

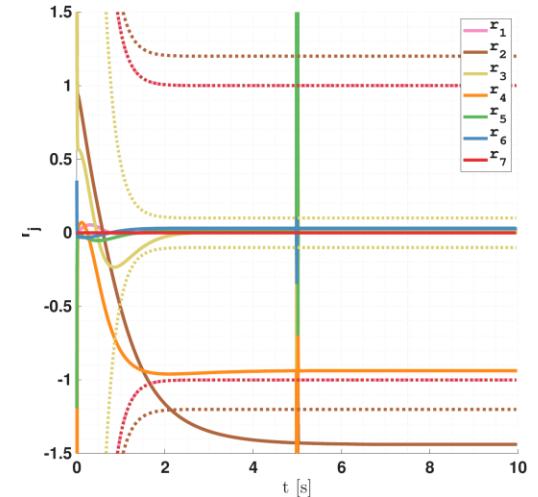
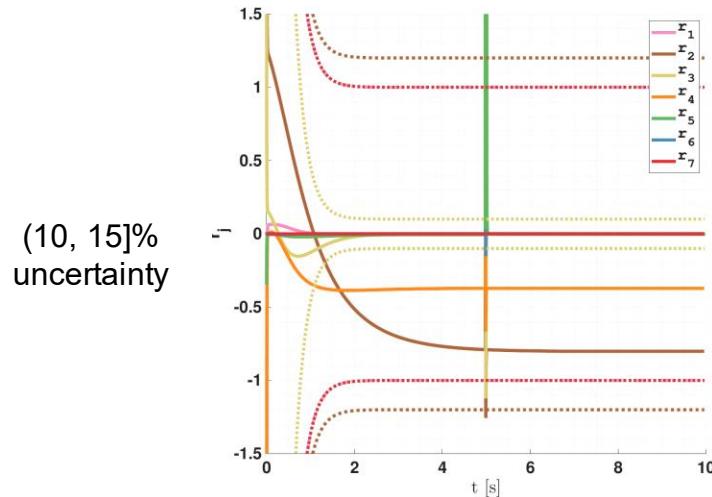
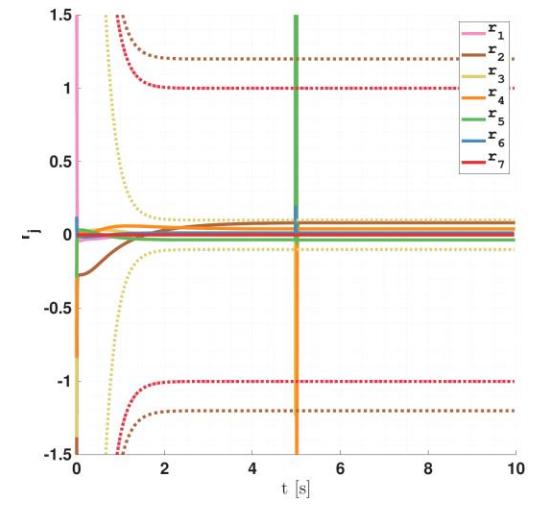
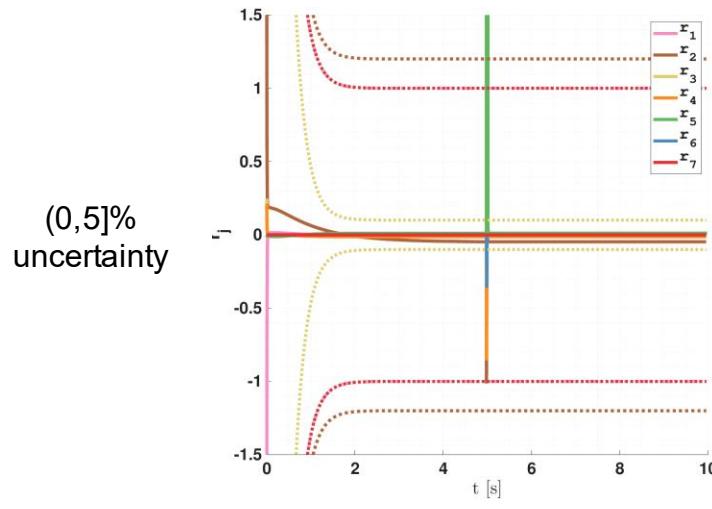


Residuals

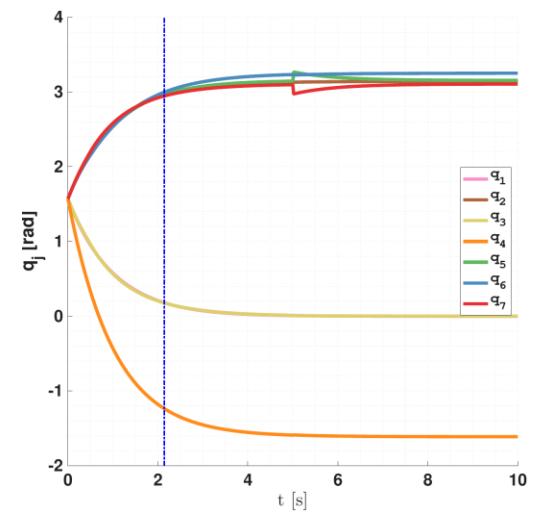
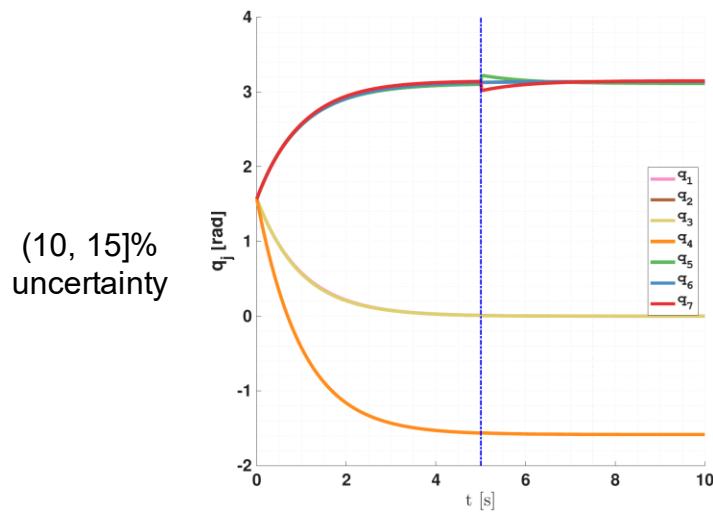
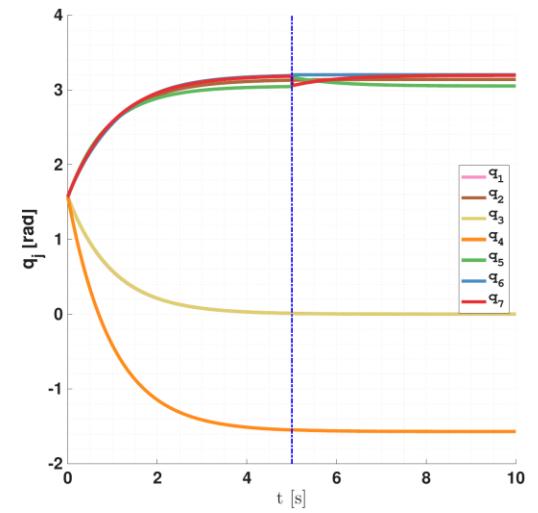
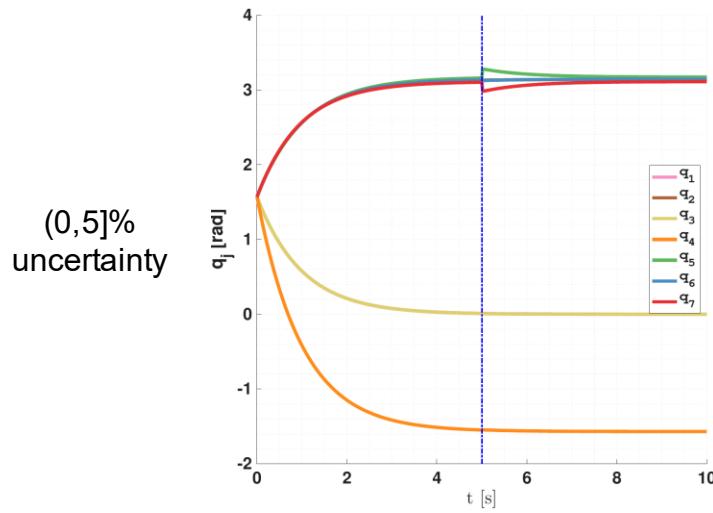
# Collision link 6 – off origin

Uncertainty	Detection time [s]	Isolated link	Estimated point [m]	Estimated force [N]	Estimated momentum [Nm]
Nominal	5.001	6	$\begin{pmatrix} 0.0509 \\ 0 \\ -0.018 \end{pmatrix}$	$\begin{pmatrix} -0.0067 \\ -9.9626 \\ 0.0659 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0.0168 \\ -0.0001 \end{pmatrix}$
0%-5%	5.001	5	$\begin{pmatrix} 0.0434 \\ 0.0036 \\ 0.0008 \end{pmatrix}$	$\begin{pmatrix} 0.8180 \\ -9.7024 \\ 0.2118 \end{pmatrix}$	$\begin{pmatrix} -0.0939 \\ 1.1341 \\ -0.0300 \end{pmatrix}$
5%-10%	5.001	5	$\begin{pmatrix} 0.0825 \\ -0.0304 \\ 0.0693 \end{pmatrix}$	$\begin{pmatrix} -2.6560 \\ -9.2421 \\ -0.6377 \end{pmatrix}$	$\begin{pmatrix} -0.9510 \\ -3.4667 \\ -0.3740 \end{pmatrix}$
10%-15%	5.001	5	$\begin{pmatrix} -0.0818 \\ -0.0064 \\ 0.0291 \end{pmatrix}$	$\begin{pmatrix} 0.8110 \\ -9.5440 \\ 0.2171 \end{pmatrix}$	$\begin{pmatrix} -0.0266 \\ 0.3097 \\ -0.0065 \end{pmatrix}$
15%-20%	2.145	2	$\begin{pmatrix} -1.0409 \\ -0.1687 \\ -5.8336 \end{pmatrix}$	$\begin{pmatrix} -0.1862 \\ -0.0340 \\ 0.0342 \end{pmatrix}$	$\begin{pmatrix} -0.0057 \\ 0.0310 \\ 0.0001 \end{pmatrix}$

# Collision link 6 – off origin (uncertain residuals)

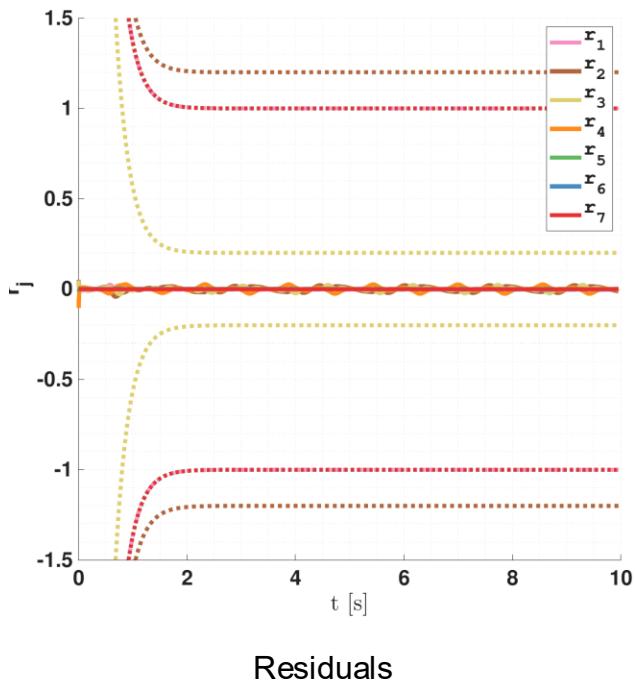
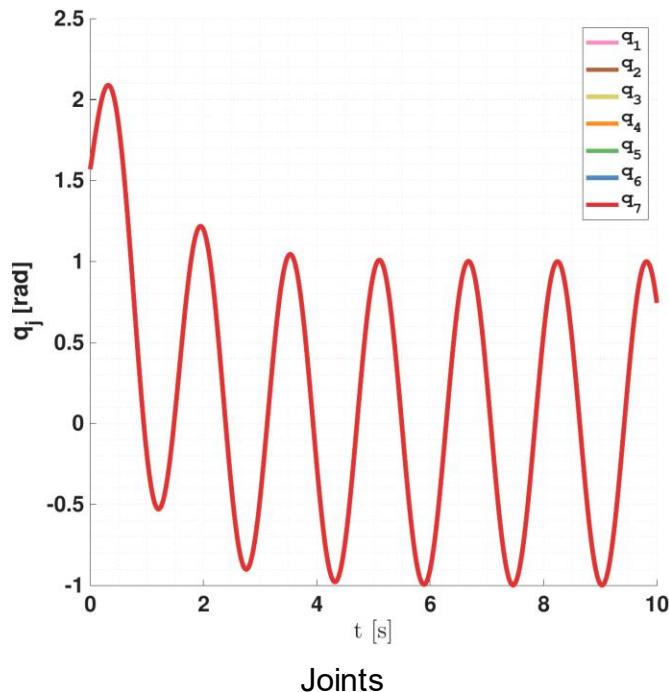


# Collision link 6 – off origin (uncertain joints)

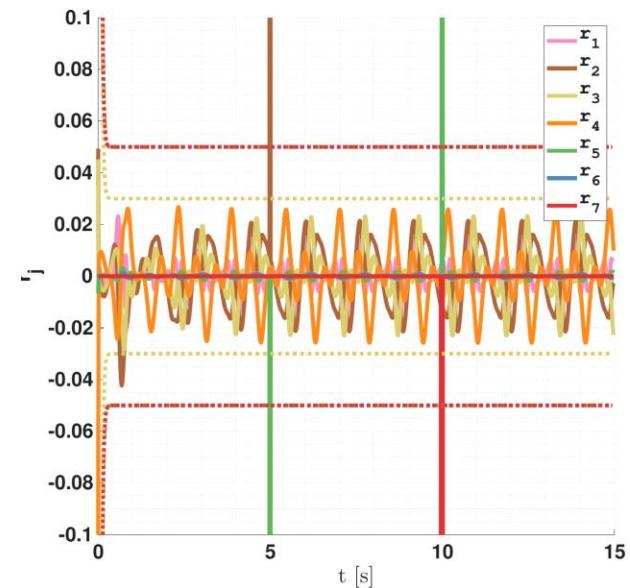
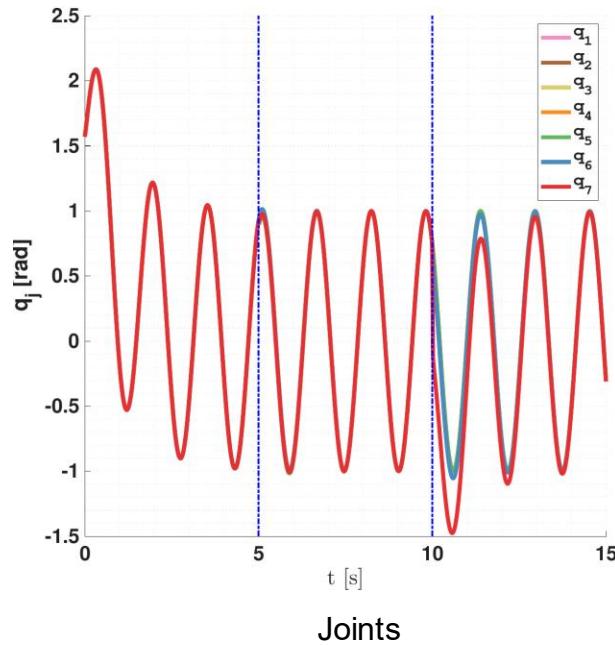


## Task 2: trajectory tracking

- Desired trajectory:  $q_{d,i} = \sin(4t)$ ,  $\dot{q}_{d,i} = 4 \cos(4t)$ ,  $\ddot{q}_{d,i} = -16 \sin(4t)$
- Initial state:  $q_0 = \left[ \frac{\pi}{2} \quad \frac{\pi}{2} \quad \frac{\pi}{2} \quad \frac{\pi}{2} \quad \frac{\pi}{2} \quad \frac{\pi}{2} \quad \frac{\pi}{2} \right]^T$



# Sequential collisions – link 5 and 7 (nominal case)



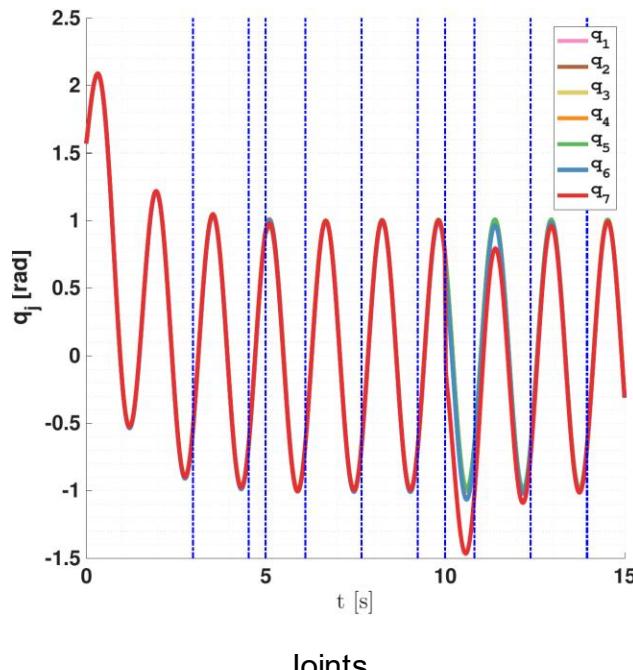
- Collisions correctly detected on link 5 at  $t=5.001$ s and on link 7 at  $t=10.001$ s
- Correct isolation and identification for link 7

$${}^0\mathbf{r}_{7,d} = \begin{bmatrix} 7.372 \\ 2.457 \\ -9.657 \end{bmatrix} \cdot 10^{-4} \text{ m}$$

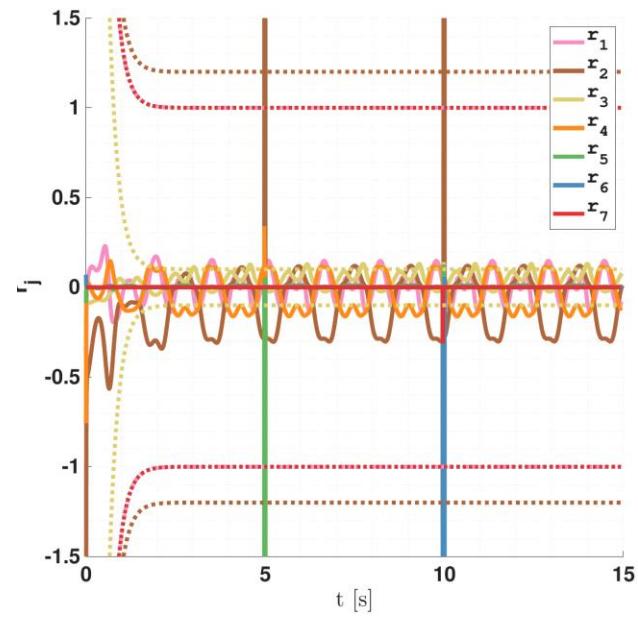
$$\hat{\mathcal{F}}_{ext} = \begin{bmatrix} 9.8748 \\ 9.8512 \\ 10.0452 \\ 0.0014 \\ 0.0014 \\ 0.0014 \end{bmatrix} \begin{bmatrix} N \\ N\text{m} \end{bmatrix}$$

# Sequential collisions – link 5 and link 7

- False positives on link 3 with just (0,5)% uncertainty



Joints



Residuals

# Conclusions

- Reliable method for collision monitoring
- Delay of 1 ms efficient for real time reactions
- Perfect behaviour in nominal case
- Performance deteriorates as uncertainty increases

## Further developments:

- Friction and actuators inertia
- Control effort and actuators saturation

# Thank you for the attention!